Orbitally forced sphalerite growth in the Upper Mississippi Valley District

M. Li¹, H.L. Barnes¹*

Abstract

Groundwater plays an important role in global water cycles and Earth’s climate system. Nevertheless, the geologic history of groundwater activity remains unclear due to limited data. Sphalerite colour banding in the Upper Mississippi Valley District (USA) is apparently caused by variation in oxidation state during precipitation which is controlled by the penetration of deeply circulating groundwater. Here, time series analysis of the grayscale profile of the Permian sphalerite banding in this district shows the banding correlates with Earth’s eccentricity, obliquity, and precession forcing. We have found that the astronomical forcing paced the fluxes of heat and precipitation and regulated the penetration of groundwater into the ore zone and thus the sphalerite banding. The results demonstrate that banding in sphalerite follows the Milankovitch climate frequencies over $10^4 – 10^5$ years. Therefore, we show that groundwater has a major role in depositing the iron-rich bands of the sphalerite and, as a final corollary, that the banding itself can be used to decipher the effects of climate on groundwater variations in the global water cycle.

Introduction

Mississippi Valley Type deposits yield about 24% of the global commercial zinc and lead resources (Leach et al., 2010). The Upper Mississippi Valley District in Iowa, Illinois and Wisconsin of the United States is typical of the lower temperature hydrothermal ores of the Mississippi Valley Type.

From extensive research by many scientists, a genetic model has been developed for the Upper Mississippi Valley District (review in Barnes, 2015). The hydrothermal fluids that carried the ore components apparently originated as ground waters high in the Southern Appalachians, a source that was elevated during the Permian by the Alleghenian Orogeny. These brines flowed northwestward about 1100 km descending through and beyond the Illinois basin (Fig. S-1). Along that geochemically tracked path, the waters became geothermally heated and collected ore solution components (Barnes, 2015). The geochemistry of the depositional reactions is consistent with a process of mixing of the geothermal solution with local groundwaters which caused oxidation and cooling of the ore-transporting fluid and precipitation of its minerals. The dominant product was sphalerite with vivid yellow-brown-black bands caused by variation in the FeS solid solution in the ZnS. The banding was found by McLimans (1977) to be remarkably similar across hundreds of square kilometres. This regularity implies that the mixing process was consistent over large areas and that the contribution to the process by hydrothermal solution flow and by areal groundwater input were surprisingly consistent. The maximum deposition depth was about 1 km, based on palaeostratigraphic reconstruction (Rowan and Goldhaber, 1996). In essence, the banding recorded variability in geochemical conditions from groundwater penetration and mixing at the depths of the depositional sites. Testing of a correlation of the banding in the sphalerite with periodicities of weather and their causes is our means of evaluating the reliability of this hypothesis.

Groundwater plays an essential role in global water cycles via feedback between groundwater and the climate system (Maher and Chamberlain, 2014). The upper 2 km of continental crust preserves approximately 22.6 million km$^3$ volume of total groundwater, which is equivalent to a 180 m deep layer of flood water if spread evenly across the global land surface (Gleeson et al., 2016). Small changes in the volume of groundwater can have significant impacts on the global water balance and lead to large sea level changes (Gleeson et al., 2016). The hypothesis of groundwater-driven sea level changes might be the most promising interpretation of high amplitude sea level changes at the $10^4-10^5$ year scale that regulated climate in the greenhouse world with no ice sheet (Wagreich et al., 2014; Li et al., 2018a). However, lack of geological evidence of groundwater activity restricted the understanding of the driving force and timing of groundwater activity and, furthermore, hampered the robustness of the sea level projection by the Intergovernmental Panel on Climate Change (IPCC) (Church et al., 2013).

The objective here is to determine the time dependence of the sphalerite banding in order to resolve the regional climate and groundwater activity in this district.
during the Permian. According to the Milankovitch theory, the Earth’s climate is affected by quasi-periodic changes in Earth orbital parameters which affect the insolation received at the top of the atmosphere at a 10^4–10^5 year scale (Laskar et al., 2004). Here, time series analysis demonstrates that oscillations of grayscale profiles of the sphalerite banding correlate with Milankovitch cycles. This study provides geological evidence that astronomical forcing had significant impact on sphalerite growth due to the oxygen activity in groundwater.

## Materials and Methods

The sphalerite sample analysed here was collected from the West Hayden orebody near Shullsburg, Wisconsin (Fig. 1). The colour banding in sphalerite is caused by variation in the FeS content of sphalerite (McLimans et al., 1980). The high grayscale value is an indication of a dark coloured mineral with a high FeS content, and vice versa (McLimans et al., 1980). A grayscale profile of sphalerite banding (Fig. 2) was digitalised and analysed using Acycle software (Li et al., 2019). In order to identify optimal deposition rate and test the null hypothesis ($H_0$) that no astronomical forcing drove oscillations of the colour banding, we ran the statistical methods of correlation coefficient (COCO) (Li et al., 2018b) and TimeOpt (Meyers, 2015). The COCO and TimeOpt methods are both designed to estimate the optimal sedimentation rate from a palaeoclimate series in stratigraphic domain and are detailed in the Supplementary Information.

The COCO results suggest the correlation coefficient value reaches the higher peak at the depositional rate of 0.27 μm/a at which the null hypothesis ($H_0$, no orbital forcing) significance level is 0.20%. There is a peak at 0.08 μm/a but the correlation coefficient is much lower than that at 0.27 μm/a. In comparison, the TimeOpt analysis indicates the highest $r_{\text{envelope}}$ peak occurs at 0.27-0.36 μm/a, the highest $r_{\text{power}}$ peak at 0.08 μm/a, and the highest $r_{\text{opt}}$ peak at 0.29-0.36 μm/a. A combination of the above analyses suggests that the optimal depositional rate of the studied sphalerite sample is probably 0.27 μm/a. Periods of Milankovitch cycles at 270 Ma were 413 kyr, 123 kyr, 95 kyr, 44.3 kyr, 35.1 kyr, 21.0, and 17.6 kyr (Berger et al., 1989). The null hypothesis can be rejected at a confidence level of 99.80% and the dominant 32 mm cycles in the banding correlate with 118.5 kyr (probably short eccentricity) cycles, and the 9.4-7.6 mm, 3.9-3.7 mm, 3.1 mm, 1.75-1.0 mm and 0.58 mm cycles are probably 34.8-28.1 kyr (obliquity), ~14 kyr (probably precession), 11.5 kyr, 6.5-3.7 kyr and 2.1 kyr (sub-Milankovitch) cycles, respectively.

## Results

Power spectral analysis of grayscale data indicate significant frequency peaks corresponding to 32 mm, 9.4-7.6 mm, 1.75 mm, 1.0 mm, and 0.58 mm cycles (Fig. 3). There are also high amplitude peaks corresponding to wavelengths at 3.9-3.7 mm and 3.1 mm. Statistical analysis using both COCO and TimeOpt methods give similar results. In Figure 4a-c, the COCO results suggest the correlation coefficient value reaches the higher peak at the depositional rate of 0.27 μm/a at which the null hypothesis ($H_0$, no orbital forcing) significance level is 0.20%. There is a peak at 0.08 μm/a but the correlation coefficient is much lower than that at 0.27 μm/a. In comparison, the TimeOpt analysis indicates the highest $r_{\text{envelope}}$ peak occurs at 0.27-0.36 μm/a, the highest $r_{\text{power}}$ peak at 0.08 μm/a, and the highest $r_{\text{opt}}$ peak at 0.29-0.36 μm/a. A combination of the above analyses suggests that the optimal depositional rate of the studied sphalerite sample is probably 0.27 μm/a. Periods of Milankovitch cycles at 270 Ma were 413 kyr, 123 kyr, 95 kyr, 44.3 kyr, 35.1 kyr, 21.0, and 17.6 kyr (Berger et al., 1989). The null hypothesis can be rejected at a confidence level of 99.80% and the dominant 32 mm cycles in the banding correlate with 118.5 kyr (probably short eccentricity) cycles, and the 9.4-7.6 mm, 3.9-3.7 mm, 3.1 mm, 1.75-1.0 mm and 0.58 mm cycles are probably 34.8-28.1 kyr (obliquity), ~14 kyr (probably precession), 11.5 kyr, 6.5-3.7 kyr and 2.1 kyr (sub-Milankovitch) cycles, respectively.


Discussion

**Sphalerite depositional process linked to groundwater flow.** Barnes (2015) concluded that inorganic complexes were insufficiently stable to carry dissolved base metals into these ores. With alternative, unspecified organic ligands L, that could have complexed the (Zn, Fe)S, a schematic reaction may be proposed for deposition by oxidation as in Sicree and Barnes (1996):

\[
x\text{ZnSL}_y + (1 - x)\text{FeSL}_x \rightarrow (\text{Zn}_x\text{Fe}_{1-x})\text{S} + x\text{Ly} - a + (1 - x)\text{L}_z - b \quad \text{Eq. 1}
\]

**Sphalerite**

The iron content of the sphalerite is set by the oxidation state of the ore solution which controls partitioning of aqueous iron species between sphalerite and pyrite as in FeS + H₂S(aq) + 0.5O₂(aq) → FeS₂ + H₂O \quad \text{Eq. 2}

In sphalerite pyrite

where the oxidation could be promoted by O₂ (often about 8 ppm in groundwater) or other oxidants. The colour banding in this sphalerite is apparently caused by the variation in oxidation state during precipitation which must be controlled by the depth penetration of circulating groundwater which is controlled by the ambient climate.

**Astronomical forcing.** The colour banding of the sphalerite from the Upper Mississippi Valley District was first suggested to be periodic by Roedder (1968). He argued that the periodic bandings are annual “varves” and reported similar “varved” samples from Belgium, Germany, Austria, Tirol, Italy, Poland and the United States and most of these “varves” have a thickness ranging from 1 to 7 μm (up to 16 μm in Moresnet, Belgium). However, from radiometric dating and modelling of diffusion and heat and flow rates, about 270 Myr ago apparently sphalerite in the Upper Mississippi Valley District was deposited for about 0.25 Myr in layers up to 5 cm total thickness at a rate of about 0.2 μm/a (Barnes, 2015); this conclusion is in agreement with an independent estimation of 0.212 Myr in duration (Rowan and Goldhaber, 1996). The depositional rate of 1-7 μm/a by Roedder (1968) is one order of magnitude higher than our result derived from statistical methods. In comparison, the depositional rate by Barnes (2015) of 0.2 μm/a is supported by our estimated depositional rate of 0.27 μm/a. An overview of similar results from other quickly deposited samples and possible modelling of the hydrothermal conditions is summarised in the Supplementary Information.

Non-hydrothermal mineral growth paced by astronomically forced climate oscillations has been reported in many Quaternary studies. For example, the Devil Hole, Nevada preserved a thick (>14 cm) layer of calcite that precipitated continuously from calcite supersaturated groundwater over the past 200 kyr with a sedimentation rate of ~0.6-1 μm/a (Moseley et al., 2016). Comparison between δ¹⁸O of calcite samples and insolation suggested that the calcite precipitated from groundwater recorded astronomically forced climate. The power spectral analysis suggests changes in the sphalerite deposition rate were dominated by eccentricity and obliquity forcing (Fig. 3). Based on the calculated sphalerite growth rate of 0.2 μm/a, high amplitude ~30 mm and 10 mm periodicities in iron content of this sample were assigned to 150 kyr and 50 kyr cycles, respectively by Mason (1987), this is roughly comparable to our interpretation. The eccentricity signal is expected because eccentricity forcing controls the extreme seasonal contrasts and thus intensity of precipitation at 10⁵ year scale. Considering the small influence of obliquity in insolation in low latitude region, such as the Upper Mississippi Valley District, the significant obliquity signal must be attributed to the indirect climate response to obliquity forcing. Actually, during the time of the sphalerite deposition at 270 Ma, the Earth was suffering the Late Palaeozoic icehouse (Montañez and Poulsen, 2013). It is widely accepted that the primary climate beat in the Cenozoic icehouse is in the obliquity band, regardless of the location.

![Figure 4](image-url)  
**Figure 4** Sphalerite deposition rate. (a) The COCO analysis shows optimal deposition rate at 0.27 μm/a. (b) Null hypothesis testing of the data series indicates that 0.08 μm/a and 0.27 μm/a deposition rates have significance levels less than 1%. (c) Number of contributing astronomical parameters. (d) Squared correlation coefficient for the amplitude envelope fit (r²-envelope) and (e) the spectral power fit (r²-power). (f) Combined envelope and spectral power fit (r²-opt) at test deposition rate.
of ice sheets and other boundary conditions; this is because the ice sheets in the polar region are sensitive to high latitude insolation that is controlled by obliquity forcing (Zachos et al., 2001). Indeed, the obliquity signal in sphalerite banding is not alone; strong obliquity signals are also recorded in a low latitude carbonate succession in South China in 262-269 Ma (Fang et al., 2017). Therefore, the interpretation of the eccentricity and obliquity signals in the sphalerite banding is that astronomically-forced flux of heat and precipitation (cf. Raymo and Nisanciglu, 2003) drove the penetration of near surface groundwater into deep groundwaters.

**Groundwater.** Deep groundwater is often not formally considered in global Earth system due to a lack of understanding of the mechanism and timescale of groundwater activity. Recent studies of groundwater in the geological past provided insight into fundamental questions such as what the missing link is for reconciling geological evidence of $10^4$-$10^6$ year scale, high amplitude sea level changes and models of eustasy change during non-glacial times, e.g., in the Early Triassic and the mid-Cretaceous (Wagreich et al., 2016; Li et al., 2018a). However, all these studies relied on indirect estimates of palaeo-lake levels as an indicator of groundwater table and are under a coarse geochronology with a resolution of $10^3$-$10^4$ year scale.

Our study suggests that globally distributed sphalerite banding provides a record of groundwater activities with an ultra-high time resolution. The maximum deposition depth of the sphalerite was about 1 km (Rowan and Goldhaber, 1996). The banding of sphalerite clearly demonstrates Milankovitch and sub-Milankovitch forcing of climate that have a significant impact on a groundwater reservoir at a depth of up to 1 km. The time to affect a groundwater reservoir significantly after changes in global hydrological cycle is hypothesised to be on the order of $10^4$ – $10^5$ years (Hay and Leslie, 1990; Li et al., 2018a). The time scale of deep groundwater activity can be on the order of $10^3$ – $10^4$ years, supporting this hypothesis.

### Conclusions

Statistical analysis of grayscale data of sphalerite in the Upper Mississippi Valley District provides constraints on the mechanism and timing of sphalerite deposition processes. The sphalerite deposition process was paced by Earth's eccentricity, obliquity, and precession forcing. We propose that the astronomical forcing paced the flux of heat and precipitation controlling the variation in oxidation state during precipitation. Astronomical forcing has significant impact on the deep (up to 1 km) groundwater at a time scale of $10^3$ – $10^5$ years. This study indicates that sphalerite banding can be used as a fingerprint of groundwater in the geological past. Groundwater is crucial for understanding global sea level change (Gleeson et al., 2016; Li et al., 2018a), chemical weathering and landscape evolution (Maher and Chamberlain, 2014), and this study helps us discern the role of groundwater in the Earth system.

### Acknowledgements

This paper evolved from Scott Mason’s exploration of this problem in his M. S. Thesis in 1987 through advances in district data and in periodicity analyses. Critical reviews of our manuscript by Antonio C. Lasaga and Andrew Sicree led to substantial improvements. We thank editor Eric H. Oelkers, Bruce Yardley, and one anonymous reviewer for their constructive comments.

**Editor:** Eric H. Oelkers

### Additional Information

**Supplementary Information** accompanies this letter at http://www.geochemicalperspectivesletters.org/article1929.

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**Cite this letter as:** Li, M., Barnes, H.L. (2019) Orbitally forced sphalerite growth in the Upper Mississippi Valley District. *Geochem. Persp. Let.* 12, 18–22.

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### References


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Supplementary Information

The Supplementary Information includes:
- Materials and Methods
- Supplementary Text
- Tables S-1 and S-2
- Figures S-1 to S-12
- Supplementary Information References

Materials and Methods

The timing of the sphalerite deposition in the Upper Mississippi Valley District (UMVD, Fig. S-1) has been dated at 270 ± 4 Ma from Rb-Sr isochrons of three sphalerite bands (Brannon et al., 1992), matching with a contemporaneous, genetically-related igneous activity in the Illinois Basin dated with average Ar-Ar age of 271.3 ± 0.6 Ma (Rowan and Goldhaber, 1996). The sample analyzed in the main text is Sample 58 of McLimans et al. (1980) (Fig. 1 as in main text). The sphalerite stratigraphy in the UMVD has been divided into three stages: A (early), B (middle), and C (late) and the studied Sample 58 represents the entire period of sphalerite deposition.

Rock colors, including grayscale, can be interpreted as qualitative measurements of climate conditions for marine and terrestrial sediments (Li et al., 2019b). The darkness of the banding correlates with the iron content of the sphalerite. Comparison between relative absorbance of transmitted light and relative FeS intensity of a sphalerite sample in the Edgerton orebody (Fig. S-2) confirmed the color of the sphalerite is related to the FeS content (McLimans et al., 1980). However, that function does not directly define the periodicities in the data. For this study, sphalerite samples were first cut and polished. Then scanning of the sphalerite digitalized the color data of the samples in the RGB (red-green-blue) format. We use a time series software Acycle 1.0 (Li et al., 2019a) to transform the RGB image in the grayscale color system. This tool converts RGB values to grayscale values by forming a weighted sum of the R, G, and B components using MatLab’s rgb2gray algorithm (https://www.mathworks.com/help/matlab/ref/rgb2gray.html): grayscale value = 0.2989 * R + 0.5870 * G + 0.1140 * B. Then the grayscale profile is extracted using the “Image Profile” function in Acycle (Li et al., 2019a). To test the reliability of the “Image Profile” function in Acycle, we also extract the grayscale profile using another software ImageJ package (Abramoff et al., 2004).

The identification of Milankovitch cycles of sphalerite deposition follows typical procedures (Li et al., 2019a). The rock color series are detrended using Acycle’s “Detrending” function subtracting a linear trend (Li et al., 2019a) so that the mean of the data is zero. The linear trend can either be a long-term climate signal or a secular change in the ore solution. The resulting data (with a zero mean) was analysed using Fourier transform methods to identify any significant periodicities (termed power spectra, which are a series of numbers giving the spectral amplitude as a function of frequency, in this case inverse distance or mm\(^{-1}\)). Here both
2π multi-taper (MTM) power spectrum and periodogram are calculated using “Spectral Analysis” function of Acycle for the grayscale series to search for dominated wavelengths of the series related to potential astronomical cycles. The significance of the MTM power spectrum of the grayscale series is shown with robust red-noise models (Mann and Lees, 1996), which is estimated using the “Spectral Analysis” function of Acycle. Gaussian bandpass filter (Kodama and Hinnov, 2015) was applied to isolate potential astronomical parameters using “Filtering” function in Acycle (Li et al., 2019a). To relate the spacing variations to time variations (and hence to Milankovitch frequencies) one must know the deposition rate of the sphalerite growth. A given deposition rate would convert the grayscale values vs. distance into grayscale values vs. time by the simple relation: \( \text{time} = \frac{\text{distance}}{\text{deposition rate}}. \)

To unravel the actual value of deposition rate, the COCO method is used, which evaluates the correlation coefficient (\( \rho \)) between power spectra of a proxy time series and an astronomical target, converting the proxy data from depth to time for a range of test sedimentation rate (Li et al., 2018). The significance of the deposition rates is evaluated by comparison to values expected from a chance correlation using Monte Carlo methods. 2000 random spectral values with random frequencies and random amplitudes were generated to compare a random (chance) correlation to the actual power spectrum of the sphalerite time series for a given deposition rate. High COCOs with high significance would prove the direct effect of Milankovitch climate variations on the formation of the sphalerite bands and thus on the formation of Mississippi Valley-Type (MVT) ore deposits.

In comparison, the TimeOpt method simultaneously estimates the eccentricity-related amplitude modulation of the precession band (measured as \( R_{\text{envelope}}^2 \)) and the concentration of spectral power at precession and eccentricity frequencies (measured as \( R_{\text{power}}^2 \)) for a range of test sedimentation rate (Meyers, 2015). The final measure of fit (\( R_{\text{opt}}^2 \)) is defined as \( R_{\text{opt}}^2 = R_{\text{envelope}}^2 \times R_{\text{power}}^2 \). The \( R_{\text{opt}}^2 \) values range from 0 to 1, and 1 is a perfect fit to the models. Test deposition rates range from 0.005 \( \mu m/a \) to 0.5 \( \mu m/a \) with a step of 0.001 \( \mu m/a \).

Based on the astronomical theory that described the gravitational effects of the Solar system, the accurate Milankovitch cycles can be calculated (Table S-1). The calculated Milankovitch cycles are currently 405 kyr, 125 kyr and 95 kyr eccentricity cycles, 55 kyr and 41 kyr obliquity cycles, 24 kyr and 19 kyr precession cycles (Laskar et al., 2004). Due to the change in the Earth-Moon distance through tidal friction, the obliquity and precession cycles have been smaller than today’s (Berger et al., 1989). At 270 Ma, periods of Milankovitch cycles were 413 kyr, 123 kyr, 95 kyr, 44.3 kyr, 35.1 kyr, 21.0 kyr, and 17.6 kyr (Berger et al., 1989), and these values are used in both COCO and TimeOpt estimation.

**Supplementary Text**

**Analyses of the time series**

In the main text, we show a time series analysis result of Acycle-generated grayscale profile of Sample 58 from West Hayden orebody. Below are similar results using ImageJ software-generated grayscale profile of Sample 58 and Acycle-generated grayscale profiles of samples collected from Hendrickson and Edgerton (Fig. 1 in the main text).

**West Hayden Orebody (ImageJ-generated grayscale profile)**

Power spectral analysis of ImageJ software-generated grayscale data (Figs. S-3 and S-4) indicates the significant frequency peaks corresponding to 35 mm, 10-8 mm, 1.78 mm, and 1.23 mm cycles (Fig. S-5). Statistical analysis using both COCO and TimeOpt methods give similar results (Fig. S-6). The COCO results suggest the correlation coefficient (\( \rho \)) value reaches the higher peak at the depositional rate of 0.300 \( \mu m/a \) at which the null hypothesis (\( H_0 \) no orbital forcing) significance level is 0.25 %. There is a peak at 0.08 \( \mu m/a \) but the \( \rho \) is a much lower than that at 0.300 \( \mu m/a \). In comparison, the TimeOpt analysis indicates the highest \( R_{\text{envelope}}^2 \) peak occurs at 0.268 \( \mu m/a \), the highest peak of \( R_{\text{power}}^2 \) at 0.082 \( \mu m/a \), and the highest \( R_{\text{opt}}^2 \) peak at 0.268 \( \mu m/a \). A combination of above analyses suggests the optimal depositional rate of the studied sphalerite sample is probably at 0.268-0.300 \( \mu m/a \). Therefore, the null hypothesis of no orbital forcing can be rejected at a confidence level of 99.75 % and the dominated 35 mm cycles are 116-130 kyr (probably short eccentricity) cycles, and the 8.76 mm and 1.78-2.13 mm cycles are probably 29-33 kyr (obliquity) and 6-4 kyr (sub-Milankovitch) cycles.

**Hendrickson Orebody**

Power spectral analysis of Acycle-generated grayscale data (Fig. S-7) of sample from the Hendrickson orebody (Figure 1, main text) indicates frequency peaks corresponding to 45 mm, 14.5-11.2 mm, 6-3.8 mm, and 1.2 mm cycles (Fig. S-8). Statistical analysis using both COCO and TimeOpt methods give similar results (Fig. S-9). The COCO results suggest the correlation coefficient (\( \rho \)) value reaches the higher peak at the depositional rate of 0.35 \( \mu m/a \) at which the null hypothesis (\( H_0 \) no orbital forcing) significance level is 0.55 %. There is a peak at 0.11 \( \mu m/a \) but the \( \rho \) is a much lower than that at 0.35 \( \mu m/a \). In comparison, the TimeOpt analysis...
indicates the highest $r^\text{envelope}$ peak occurs at 0.35 $\mu$m/a, the highest peak of $r^\text{power}$ at 0.12 $\mu$m/a, and the highest $r^\text{opt}$ peak at 0.35 $\mu$m/a. A combination of above analyses suggests the optimal depositional rate of the sphalerite sample from the Hendrickson orebody is probably at 0.35 $\mu$m/a. Therefore, the null hypothesis of no orbital forcing can be rejected at a confidence level of 99.45 % and the dominated 45 mm cycles are 129 kyr (probably short eccentricity) cycles, and the 14.5-11.2 mm, 6 mm, 3.8 mm, and 1.2 mm cycles are probably 41-32 kyr (obliquity), 17.1 kyr (precession), 11 kyr, and 3.4 kyr (sub-Milankovitch) cycles.

**Edgerton Orebody**

Power spectral analysis of Acycle-generated grayscale data (Fig. 5-S10) of sample from the Edgerton orebody (Figure 1, main text) indicates the significant frequency peaks corresponding to 13.8 mm and 1.2 mm and other peaks at 25.6 mm, 9.4-6.9 mm, and 3.5 mm cycles (Fig. 5-S11). Statistical analysis of this shorter grayscale series using both COCO and TimeOpt methods give slightly different results (Fig. 5-S12). The COCO results suggest the correlation coefficient ($\rho$) value reaches the highest peak at the depositional rate of 0.21 $\mu$m/a at which the null hypothesis ($H_0$, no orbital forcing) significance level is 0.05 %. There is a peak at 0.07 $\mu$m/a but the $\rho$ is a much lower than that at 0.21 $\mu$m/a. In comparison, the TimeOpt analysis indicates the highest $r^\text{envelope}$ peak occurs at 0.27 $\mu$m/a, the highest peak of $r^\text{power}$ at ~0.07 $\mu$m/a, and the highest $r^\text{opt}$ peak at 0.27 $\mu$m/a. A combination of above analyses suggests the optimal depositional rate of the sphalerite sample from the Hendrickson orebody is probably at 0.21-0.27 $\mu$m/a. Therefore, the null hypothesis of no orbital forcing can be rejected at a confidence level of 99.45 % and the dominant 13.8 mm and 1.2 mm cycles are 66-51 kyr and 5.7-4 kyr cycles, respectively. And the high amplitude cycles of 25.6 mm, 9.4-6.9 mm, 3.5 mm cycles are probably 122-95 kyr (short eccentricity), 45-26 kyr (obliquity), and 17-13 kyr (precession) cycles.

**Deposition rates**

There is a peak deposition rate at 0.08 $\mu$m/a for the sample from the West Hayden Site (Figs. 4 and S-6). There are also comparable peaks at 0.11 $\mu$m/a at the Hendrickson Site (Fig. 5-S9) and 0.07 $\mu$m/a at Edgerton Site (Fig. 5-S12). Take the West Hayden sample as an example, if the deposition rate at 0.08 $\mu$m/a instead of 0.27 $\mu$m/a is used, then the dominant periodicities are 400 kyr, 117.5-95 kyr, 21.9-12.5 kyr, and 7.3 kyr. These compare with the Peruvian Milankovitch cycles listed above. However, there are three lines of evidence that support the 0.27 $\mu$m/a rather than 0.08 $\mu$m/a deposition rate in this case. First, as shown in Figure 4a, the correlation coefficient at 0.27 $\mu$m/a is much higher than that at 0.08 $\mu$m/a suggesting that the deposition rate at 0.27 $\mu$m/a has a much better fit than at 0.08 $\mu$m/a. Second, the TimeOpt analysis indicates the highest $r^\text{envelope}$ peak occurs at 0.27-0.36 $\mu$m/a and no peak at 0.08 $\mu$m/a, and the highest $r^\text{opt}$ peak at 0.29-0.36 $\mu$m/a and very low peak at 0.08 $\mu$m/a. A combination of information from precession amplitude and power spectra suggests the optimal depositional rate of the studied sphalerite sample is probably 0.27 $\mu$m/a. Third, from radiometric dating and modeling of diffusion and heat and flow rates, apparently sphalerite was deposited for about 0.25 My in layers up to 5 cm maximum thickness at a rate of about 0.2 $\mu$m/a (Barnes, 2015), this conclusion is in agreement with an independent estimation of 0.212 Myr in duration (Rowan and Goldhaber, 1996). In sum, the deposition rates of these sites are 0.27 $\mu$m/a at West Hayden, 0.35 $\mu$m/a at Hendrickson, and 0.21-0.27 $\mu$m/a at Edgerton.

The depositional rate of 1-7 $\mu$m/a by Roedder (1968) is one order of magnitude higher than our result derived from statistical methods. The varves recognized by Roedder (1968) are probably decadal, not annual, varves.

**Variable deposition rate vs. constant deposition rate**

COCO analysis of synthetic series and real proxy data with constant and variable sedimentation rates suggests the COCO analysis result is insensitive to sedimentation rate changes (Li et al., 2018). The COCO aided with the sliding procedure enables the evolutionary COCO analysis, which is designed for detecting variable sedimentation rate. For example, COCO analysis of a synthetic series (#2 in Li et al., 2018; with modeled 4 and 6 cm/kyr sedimentation rates) shows strong peaks at 4 and 6 cm/kyr. COCO analysis of Fe series at Ocean Drilling Program (ODP) site 1262 indicates multiple peaks at 1.21, 0.98, and 0.73 cm/kyr, all of which are confirmed by higher resolution eCOCO analysis result (Li et al., 2018). In comparison, COCO analysis of the Triassic Newark depth rank series shows a single broad peak at 15 cm/kyr, this is also confirmed by eCOCO result that suggests the sedimentation rates throughout the series are generally stable at ~15 cm/kyr (Li et al., 2018). COCO analysis does not apply to the grayscale series in this study, because it requires the time series data long enough to allow for the sliding window procedure and each sliding window can cover sufficient data to correctly recognize the optimal deposition rate. However, the single broad peak at 0.27 $\mu$m/a from COCO analysis of the sphalerite samples from West Hayden (Fig. 4a, main text) suggests that the actual deposition rate varies a little bit and centers at 0.27 $\mu$m/a. The same argument holds for other COCO results for other samples. Therefore, the non-constant deposition rate won’t affect the conclusion of this paper.
Precipitation rates

Lasaga (1984) has precipitation rates for several silicates likely to be hydrothermally deposited. Recalculating his data from Table 5 shows that our 0.2 μm/a is roughly in the middle of his range from 0.003 to 600 μm/a (Table S-2). Our rate is also comparable to the precipitation rate of the calcite (~0.6-1 μm/a) that precipitated from calcite-supersaturated groundwater over the past 200 kyr from the Devil Hole, Nevada (Moseley et al., 2016).

Hydrothermal Modeling

The Illinois Basin in the Permian provided the Mississippi Valley Type deposits (MVTD) ore solutions after deep basin heating apparently by both igneous and mantle sources. Currently or in the past, analogous basins might generate such deposits by providing outflow of organic-rich solutions at depths of about 5 km with >100 ppm Zn, 150 - 250 °C for flow persistence >~0.5 Myr (Barnes, 2015). In the United States, of 17 basins examined for potential thermal or petroleum production, only 3, the Anadarko, Uinta, and Green River Basins are now warm enough (Anderson, 2013). Data from 49 basins globally that may be MVTD-productive have been compiled by Nelson and Kibler (2003). Searches of older basins with the pertinent characteristics could be bases for an exploration program.

Supplementary Tables

Table S-1 Astronomical periodicities in thousand years: at present (from Laskar et al., 2004) versus Permian time (270 million years ago, from Berger et al., 1989).

<table>
<thead>
<tr>
<th>From banding in sphalerite</th>
<th>From astronomical solutions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Eccentricity</td>
<td>Obliquity</td>
</tr>
<tr>
<td>At present</td>
<td>Permian</td>
</tr>
<tr>
<td>405</td>
<td>413</td>
</tr>
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<td>125</td>
<td>123</td>
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<td>95</td>
<td>95</td>
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<td>34.8</td>
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<td>14</td>
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</tbody>
</table>

Table S-2 Precipitation rates for several silicates likely to be hydrothermally deposited (from Lasaga, 1984).

<table>
<thead>
<tr>
<th>Mineral</th>
<th>Precipitation rates (μm/a)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Forsterite</td>
<td>600</td>
</tr>
<tr>
<td>K-feldspar</td>
<td>520</td>
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<tr>
<td>Albite</td>
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<tr>
<td>Enstatite</td>
<td>8.8</td>
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<tr>
<td>Diopside</td>
<td>6</td>
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<tr>
<td>Nepheline</td>
<td>0.21</td>
</tr>
<tr>
<td>Anorthite</td>
<td>0.11</td>
</tr>
<tr>
<td>Quartz</td>
<td>0.034</td>
</tr>
<tr>
<td>Muscovite</td>
<td>0.003</td>
</tr>
</tbody>
</table>
Supplementary Figures

**Figure S-1**  Schematic model of water flow from the elevated South Appalachians through the Illinois Basin to the Upper Mississippi Valley District (UMVD). Both (a) and (b) are based on Bethke (1986) and summary in Barnes (2015).
**Figure S-2**  Relative absorbance of transmitted light (solid red line) versus relative FeS intensity (dashed black line) for a portion of the sample in the Edgerton orebody (McLimans et al., 1980). Color of sphalerite is nearly black at maximum absorption (10) and nearly white at minimum absorption (0).

**Figure S-3**  Image of sphalerite sample in *ImageJ* software from the West Hyden Orebody. Colored photographs are shown with three growth stages of A (early), B (middle), and C (late) following McLimans et al. (1980). The rock colour grayscale profile was measured along the traverse (yellow line). Length of the line of a-a' is 20 mm.
**Figure S-4**  Grayscale of the sphalerite (black) and its linear trend (purple). Detrended data (gray) are shown with its 35 mm (blue) and 8 mm (red) Gauss bandpass-filtered cycles (passband: 0.028 $\pm$ 0.008 and 0.12 $\pm$ 0.08 cycles/mm, respectively).

**Figure S-5**  2n MTM power spectrum (thin black) and periodogram (gray) of the grayscale series shown with robust red-noise models. The red-noise fit to the spectrum is based on the best fit to the log power of the 20 % median-smoothed spectrum (dashed pink). The 90 % (solid red), 95 % (dashed red), 99 % (blue dashed line), and 99.9 % (dot green) confidence limits are shown. Cycle wavelengths are also marked.
Figure S-6  Sphalerite deposition rate. (a) The COCO analysis shows optimal deposition rate at 0.30 μm/a. (b) Null hypothesis testing of the data series indicates that 0.08 μm/a and 0.30 μm/a deposition rate have significance levels less than 1%. Significance levels are estimated using Monte Carlo simulations of 2000 iterations. (c) Number of contributing astronomical parameters in the test deposition rate ranging from 0.001 to 0.35 μm/a with a step of 0.001 μm/a. (d) Squared correlation coefficient for the amplitude envelope fit ($r^2_{\text{envelope}}$) and the spectral power fit ($r^2_{\text{power}}$) at test deposition rate ranging from 0.001 to 0.35 μm/a with 200 steps. (e) Combined envelope and spectral power fit ($r^2_{\text{opt}}$) at test deposition rate indicating the optimal deposition rate of 0.268 μm/a.
Figure S-7  Grayscale of the sphalerite from Hendrickson orebody (blue) and its linear trend (red) shown with detrended data (black).
Figure S-8  2π MTM power spectrum (upper panel) and periodogram (lower panel) of the grayscale series of the sphalerite sample from Hendrickson orebody (Fig. 1, main text) shown with robust red-noise models. The red-noise fit to the spectrum is based on the best fit to the log power of the 25% median-smoothed spectrum (dashed pink). The 90% (solid red), 95% (dashed red), 99% (blue dashed line), and 99.9% (dot green) confidence limits are shown. Cycle wavelengths are also marked.
Figure S-9  Sphalerite deposition rate. (a) The COCO analysis shows optimal deposition rate at 0.35 μm/a. (b) Null hypothesis testing of the data series indicates that 0.11 μm/a and 0.33 μm/a deposition rate have significance levels less than 1 %. (c) Number of contributing astronomical parameters in the test deposition rate ranging from 0.005 to 0.5 with a step of 0.001 μm/a. (d) Squared correlation coefficient for the amplitude envelope fit ($r^2_{envelope}$) and (e) the spectral power fit ($r^2_{power}$). (f) Combined envelope and spectral power fit ($r^2_{opt}$) at test deposition rate indicating the optimal deposition rate of 0.35 μm/a.
Figure S-10 Grayscale of the sphalerite from Edgerton orebody (blue) and its linear trend (red) shown with detrended data (black).
Figure S11  2π MTM power spectrum (upper panel) and periodogram (lower panel) of the grayscale series of the sphalerite sample from Edgerton orebody (Fig. 1, main text) shown with robust red-noise models. The red-noise fit to the spectrum is based on the best fit to the log power of the 25 % median-smoothed spectrum (dashed pink). The 90 % (solid red), 95 % (dashed red), 99 % (blue dashed line), and 99.9 % (dot green) confidence limits are shown. Cycle wavelengths are also marked.
Figure S-12 Sphalerite deposition rate. (a) The COCO analysis shows optimal deposition rate at 0.21 μm/a. (b) Null hypothesis testing of the data series indicates that 0.07 μm/a and 0.21 μm/a deposition rate have significance levels less than 1 %. Significance levels are estimated using Monte Carlo simulations of 2000 iterations. (c) Number of contributing astronomical parameters in the test deposition rate ranging from 0.005 to 0.5 with a step of 0.001 μm/a. (d) Squared correlation coefficient for the amplitude envelope fit ($r^2_{\text{envelope}}$) indicating the optimal deposition rate of 0.21 μm/a and (e) the spectral power fit ($r^2_{\text{power}}$) at test deposition rate. (f) Combined envelope and spectral power fit ($r^2_{\text{opt}}$) at test deposition rate.

Supplementary Information References


